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Comparison of a centralised and distributed approach for a generic scheduling system

Authors: Kieran Greer · JohnRea Stewart · Barry McCollum

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Abstract	PEGS (Production and Environmental Generic Scheduler) is a generic production scheduler that produces good schedules over a wide range of problems. It is centralised, using search strategies with the Shifting Bottleneck algorithm. We have also developed an alternative distributed approach using software agents. In some cases this reduces run times by a factor of 10 or more. In most cases, the agent-based program also	

produces good solutions for published benchmark data, and the short run times make our program useful for a large range of problems. Test results show that the agents can produce schedules comparable to the best found so far for some benchmark datasets and actually better schedules than PEGS on our own random datasets. The flexibility that agents can provide for today's dynamic scheduling is also appealing. We suggest that in this sort of generic or commercial system, the agent-based approach is a good alternative.

Keywords (separated by '-') Scheduling - Software agents - Distributed scheduling - Production scheduling - Environmental constraints

Footnote Information

Comparison of a centralised and distributed approach for a generic scheduling system

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Abstract PEGS (Production and Environmental Generic Scheduler) is a generic production scheduler that produces good schedules over a wide range of problems. It is centralised, using search strategies with the Shifting Bottleneck algorithm. We have also developed an alternative distributed approach using software agents. In some cases this reduces run times by a factor of 10 or more. In most cases, the agent-based program also produces good solutions for published benchmark data, and the short run times make our program useful for a large range of problems. Test results show that the agents can produce schedules comparable to the best found so far for some benchmark datasets and actually better schedules than PEGS on our own random datasets. The flexibility that agents can provide for today's dynamic scheduling is also appealing. We suggest that in this sort of generic or commercial system, the agent-based approach is a good alternative.

Keywords Scheduling · Software agents · Distributed scheduling · Production scheduling · Environmental constraints

Introduction

PEGS (Production and Environmental Generic Scheduler) is a generic production scheduling system developed at the Queen's University of Belfast. In addition to conventional time-based optimisation, PEGS calculations may be based on economic values and this allows consideration of any environmental effects to which a cost can be assigned. For example, waste generated at product change-overs or the varying costs of electricity at different times may be included. PEGS allows the use of multiple objectives, setup times and a wide range of constraints. These features mean that the program may be used to generate schedules for many different manufacturing models including single machine, parallel machines, flow shops and job shops. A full description of the program and comparisons of its performance on a variety of benchmark tests are given in Greer et al. (2006).

In this paper, we describe some recent work to develop a distributed algorithm, using software agents, and compare the new version of the program with the original centralised algorithm using some randomised datasets and published benchmarks. For convenience here we will refer to the original version as PEGS and the new version as PEGSagent.

In PEGS we use search heuristics together with the Shifting Bottleneck algorithm (Adams et al. 1988). In this approach all machines are considered together and a schedule is calculated from a single centralised algorithm. This approach can produce good quality solutions, but today's systems also need to be very flexible. A flexible system may cope with situations where machines are distributed across

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49 different sites, with machine breakdowns, or with agile manu-
 50 facturing methods (He and Babayan 2002). A distributed
 51 approach may be preferred because of its greater flexibility. It
 52 appears, from the lack of published comparisons, that it may
 53 be difficult to achieve the same quality of solution (schedule)
 54 using distributed methods. For PEGSAgent we have imple-
 55 mented and tested a distributed approach using agent-based
 56 technology. In the remainder of this paper we present some
 57 comparisons between the two different approaches. We have
 58 not found published details of similar comparisons elsew-
 59 here, either considering a generic or a specialised system.

60 Software agents have now been widely used in scheduling,
 61 see Shen (2002) for a summary. An agent-based approach is
 62 a distributed approach, where complex problems are broken
 63 down into a number of simpler problems which are distribu-
 64 ted among several agents. The agents then attempt to solve
 65 the simpler problems and their combined efforts will produce
 66 a solution to the global problem. Jennings (2000) outlines
 67 the advantages of using an agent-based approach to software
 68 engineering. There are various features that an agent should
 69 possess. One of these is that an agent should be autonomous
 70 or semi-autonomous. This means that it has its own internal
 71 control system and is able to make independent decisions on
 72 behalf of the user. An autonomous agent is also pro-active and
 73 may initiate other processes. Agents communicate with each
 74 other using an agent communication language. The Founda-
 75 tion for Intelligent Physical Agents, FIPA, is the organisation
 76 responsible for creating standards for agent-based technol-
 77 ogy and its Agent Communication Language is called ACL.
 78 Agents use ACL to pass messages to other agents telling
 79 them what to do. The message passing protocols are also
 80 standardised. Our agents are semi-autonomous in that they
 81 generate a schedule independently once they have been asked
 82 to do so. They communicate using the standard communi-
 83 cation protocols Contract Net and Query Ref (FIPA 2002),
 84 plus an even simpler protocol that just asks an agent to do
 85 something.

86 The Contract Net protocol is a standard bidding protocol.
 87 It is used to allow agents to bid with each other to provide
 88 a service for some other agent. In our case we allow the
 89 machine agents to compete with each other to provide a time
 90 slot in which to complete an operation belonging to some
 91 job. Query Ref is much simpler and is used to send a query
 92 from one agent to another and then receive a reply from that
 93 agent. We have written our own agent platform, agents and
 94 protocols, etc. so that they could be customised to our own
 95 specific problem. However, we expect that the protocols used
 96 here could equally have been implemented using an open-
 97 source generic agent platform.

98 In the remainder of this paper we describe some related
 99 work on centralised and distributed systems (Section “Rela-
 100 ted work”), the main features of our system (Sec-
 101 tion “Main features”), the architecture of our centralised

(Section “Centralised architecture”) and distributed systems
 (Section “Distributed architecture”), a comparison with other
 systems (Section “Comparison with other systems”), a com-
 parison of the two program versions on a series of tests (Sec-
 tion “Testing the two approaches”), and some conclusions
 (Section “Conclusion”).

Related work

Search algorithms

PEGS provides a choice from three different search algo-
 rithms to find a solution: tabu search (Hertz et al. 1992;
 Morton and Pentico 1993; Pinedo 2002; Nowicki and Smut-
 nicki 1996), simulated annealing (Pinedo 2002) and beam
 search (Pinedo 2002; Valente and Alves 2004).

Tabu search and simulated annealing are both nearest
 neighbour search strategies. They begin with some initial
 ordering (a schedule) and then make a change to it in the
 close neighbourhood of that ordering. If the changed order-
 ing is better it is retained as the current best solution and a
 new modification is made from that one. If the change is not
 an improvement, then a different modification is made from
 the original ordering. The program continues making modi-
 fications and evaluating the results until a specified number
 of iterations have elapsed or time has run out. If the only
 next moves are those which give a worse solution then it is
 possible to be trapped in a local optimum (a region of the
 search space where no immediate near neighbour move will
 provide a better solution, even though there may be better
 solutions in some other area of the search space). In this case
 it may be necessary to allow a move to a worse solution in
 order to move out of a local optimum, so that an even better
 global optimum may be found. Tabu search and simulated
 annealing have mechanisms in place to allow this.

In tabu search a record is kept of the last m moves made in a
 tabu list. Making a reverse of these moves while they are in the
 list is not allowed. This will prevent repeated cycling between
 two moves, but may mean it is occasionally necessary to
 make a worse move (that is not in the list) before it becomes
 possible to again find better moves. The actual moves made
 are generated randomly, typically by choosing two operations
 at random and swapping their positions to produce a new
 candidate solution. For the first half of the search we swap
 any two operations, while for the second half we swap just
 neighbouring operations.

Simulated annealing provides a probability function,
 where a worse move may be made at certain iterations with a
 pre-determined probability. This also means that if the solu-
 tion is trapped in a local optimum there is an opportunity of
 moving out of it again. Simulated annealing has a ‘cooling
 factor’ which is used to determine how often the probability

function will allow a worse move. Initially the cooling factor is set quite high and worse moves are permitted more often. As the number of iterations completed increases, the cooling factor is decreased, making it less likely that a move to a worse solution will be allowed. This has the effect of allowing the search strategy to roam widely at the start and then settle on a particular area of the search space as the number of iterations increases. The basic algorithms for these search strategies are described in Pinedo (2002). The tabu search algorithm has been modified to include an aspiration criterion (see Chambers and Barnes 1996). If a move is made that results in a better solution than any found so far, even if it is tabu, the move is still allowed.

Beam search is a breadth-first search that prunes nodes at each level of a search tree. From each solution at one level, all possible next solutions are generated by swapping elements (operations) with one of the elements in the original solution. This produces a new number of solutions at a new level of the search tree. These new solutions can then be expanded in the same way, until all swaps have been considered. The basic algorithm is again taken from Pinedo (2002). Starting from an initial ordering, changes are made by swapping all elements with the first one. This will produce a number of new solutions. Each new solution is evaluated and a certain number, as specified by the beam width, are retained. If, for example, the beam width is 10, only the 10 best new solutions are kept. These new solutions are then expanded again by swapping all elements (except for the first one) with the second element. These new solutions are evaluated again and a beam width number kept, and so on until all of the elements in the solution have been swapped. The algorithm will generate all of the possible solutions, except for those pruned (or rejected) by the beam width. It is also possible to include a filter width, where an initial evaluation of new solutions is made, based on a relatively simple evaluation function, and a filter width number of these are retained. This filter width number is subsequently evaluated using a more sophisticated function and a beam width number of these are retained.

There is also an exhaustive branch and bound algorithm for simple testing that considers all possible solutions. This is, of course, far too slow to use on problems of a realistic size.

The Shifting Bottleneck algorithm

The Shifting Bottleneck algorithm is used for job shop or flow shop configurations. This is a well tried and trusted algorithm that was originally suggested in Adams et al. (1988) and is also in Balas and Vazacopoulos (1998). It is known to be reasonably fast and to produce good quality solutions. Various authors have produced optimal solutions for benchmark datasets using specialised algorithms coupled with the Shifting Bottleneck algorithm. Our system is generic using the search

strategies described in Section “Search algorithms” with the Shifting Bottleneck algorithm and thereby producing reasonable results for a wide range of problems.

The Shifting Bottleneck algorithm works by finding the bottlenecks in the system. These are the machines or workcentres responsible for the greatest delay to the schedule. Preference is given to these areas by generating their schedules first. This approach tends to generate schedules most favourable to the bottleneck operations/machines. In the Shifting Bottleneck algorithm, during each iteration, it is necessary to find the worst bottleneck. This is the workcentre that is producing the worst evaluation. A workcentre is a group of one or more machines, all running in parallel, that can process the same operations. A schedule is generated for each workcentre using initial available times. The workcentre with the worst objective is taken as the worst bottleneck. This bottleneck is then optimised first in the next iteration, which means that its allocation of operations to time slots are given preference over all other bottleneck allocations. When the operations have been allocated, the other bottlenecks’ allocations are adjusted based on these and optimised in turn. Next the second worst bottleneck is identified as the worst of the remaining bottlenecks. The first and second worst bottlenecks are then balanced together. This means optimising the first worst bottleneck, then the second worst bottleneck (updating allocation times in the process), and repeating until there are no changes in their evaluations or a specified number of iterations have passed. When these bottlenecks have been balanced, the allocation times in the remaining bottlenecks are updated and evaluated in turn to determine the third worst bottleneck. The three worst bottlenecks are then balanced and the process is repeated until all bottlenecks have been balanced.

Together, the search and shifting bottleneck algorithms represent a centralised approach to the scheduling problem. In the next sections we describe an alternative approach using agent technology.

Agent-based systems

There has been a move towards a distributed solution to the production scheduling problem because it is more flexible and adaptable to changes that may occur in day-to-day scheduling. There is now a substantial body of literature on agent-based systems used as distributed production scheduling systems. Babiceanu and Chen (2006) survey the current status of distributed manufacturing systems, including agent-based technology in production scheduling. One advantage of this approach is its ability to cope with dynamic changes such as machine breakdowns, new orders or changes in existing orders; a flexibility sometimes described as agile manufacturing (He and Babayan 2002; Boccalatte et al. 2004). If, for example, each machine is represented by a separate agent,

it is easier to simply remove a machine if it breaks down, or keep parts of the schedule the same while allowing other parts to be changed by fixing certain agents and allowing others to be re-scheduled. If it is only necessary to re-schedule part of the system, it can be done much more quickly with an agent-based approach. Shen and Norrie (1998) describe their MetaMorph II system which attempts to address these issues. Yoo and Muller (2002) also address the dynamic job shop scheduling problem. Shen (2002) provides a tutorial which describes the problems that agents address and also lists some systems. Walker et al. (2005) describe an agent-based system that uses evolutionary algorithms to evolve a scheduler rather than the schedule itself. Globally dispersed manufacturing enterprises need to address issues of accessibility, integration and re-configurability (Yen 1998). Planning is usually integrated with the scheduling and changing product specifications or shop floor configurations need to be quickly integrated into the system. To tackle this problem, the planners and schedulers may be involved in some sort of communication. An agent-based approach can prove a good match to this kind of problem as it already relies on multiple inter-agent communications. PEGSAgent is only concerned with the scheduling phase, but an agent-based approach may be more easily extended to cope with planning problems as well.

Another feature of agent-based systems is the potential to introduce a bidding mechanism. This means that it is possible to change the evaluation from a time-based one to an economic-based one, or possibly include time-based and economic-based factors in a single evaluation (however, our centralised system also has some experimental economic objectives that can be used). Dang and Frankovic (2002) introduce a system that is cost-based and copes with a flexible manufacturing environment. Wellman et al. (2003) explore a number of different bidding strategies. Other systems that involve bidding include Lim and Zhang (2002), Boccalatte et al. (2004) and Vancza and Markus (2000). Parunak et al. (1998) describe a comparison between agent-based modelling and equation-based modelling for supply networks and note advantages for each approach.

Main features

This section briefly describes the main features that PEGS provides. These features are available in both the centralised and distributed versions. A demo version of the program is available for downloading from our Environmental Modelling Group website (Stewart 2006).

The program allows for static or dynamic ready times and can attempt to minimise the amount of idleness in the schedule. The program allows setup times to be entered for each operation or for families of operations.

There are a variety of constraints. Operation constraints allow the user to constrain one operation to be beside or before another operation. If one operation is constrained to be beside another, then they are scheduled together on the same machine. Section "Centralised architecture" describes the centralised architecture, where for each workcentre, there is a single machine schedule generated before the operations are assigned to the parallel machines. This single machine schedule determines the order in which the operations are assigned to the parallel machines. We also have a weak form of the beside constraint, where the operations are constrained to be beside each other in the single machine schedule but can then be separated when assigned to the parallel machines. This has the effect of scheduling them at times close to each other but not necessarily on the same machine. Time-based constraints include shift times or any other time period when a machine is not available. If using shift times, it is possible to specify a preference that operations be completed on the same shift in which they started. There are also resource constraints where a maximum available quantity can be specified and the sum of the amounts consumed by the machines in use cannot exceed this. Typical resources include energy used by the machines or the number of operators required to run the machines.

It is also possible to use environmental constraints. The value of waste produced by an operation change-over may be entered for each operation or for families of operations. Energy tariffs, varying with time of day and calendar, may be entered and included. As waste and energy are measured in monetary units, an objective based on economic values rather than time-based values is then used. It is also possible to use cost-based objectives by entering cost estimates for factors such as the cost to process an operation on a machine per unit time. Then the time-based objectives can be converted into cost-based ones using a number of simple but experimental conversion equations we have developed.

We permit operations for the same product to overlap rather than to take place in strict sequence. The default is strictly sequential, assuming that each operation requires as input the output from the previous one. However, it will sometimes be the case that operations are independent of each other and can overlap in time on the same group of parallel machines or different groups of machines. Overlapping can be switched on or off for different operations required for a particular job. We also allow the user to fix the operation time or the machine an operation should be run on. We have provided for buffers between each operation which may accumulate stock as it is produced. Users may specify any batch amount by which the items may then be removed from a buffer. We have also implemented a special 'accumulation' operation. Users may group a number of operations from different jobs into a single operation on a notional machine and process them as a single operation. This feature would be

356 useful in a pottery or bakery where different items would be
 357 processed together in a single oven. It was actually imple-
 358 mented for a furniture manufacturer which makes various
 359 components at one site and then transports them to another
 360 for subsequent assembly. The transport step is treated as an
 361 accumulation operation.

362 The generated schedules are displayed on an interactive
 363 Gantt chart. This is colour-coded with respect to job or oper-
 364 ation type. The user can use a key to highlight individual
 365 operations in selected jobs and enlarge/shrink the chart. The
 366 user can manually move operations to new machines/relative
 367 positions and re-schedule, or can fix operation positions and
 368 re-schedule round them. The user can also remove operations
 369 scheduled before a certain time and re-schedule the rest.
 370 This feature is also available from the main window, where
 371 the user can enter new job specifications and combine them
 372 with an existing schedule, removing operations already com-
 373 pleted from the existing schedule. The schedule is also
 374 displayed in a textual format. This can be as a report that
 375 describes the schedule in relatively simple terms, or you can
 376 also have a full description of the scheduling details, that can
 377 actually be used to re-construct the schedule.

378 We have also developed a version of the centralised archi-
 379 tecture that can be physically distributed. Each workcentre
 380 scheduling process of the shifting bottleneck algorithm can
 381 be run on a different machine in parallel, thus speeding up
 382 processing time. Results showed that the schedule quality
 383 was almost the same, while the scheduling times were much
 384 faster. For example, using three computers could speed sched-
 385 uling up by a factor of nearly three.

386 **Centralised architecture**

387 The PEGS scheduling system uses a relatively straightfor-
 388 ward architecture, as illustrated in Fig. 1 (previously given
 389 in Greer et al. 2006). The three main algorithms used in the
 390 process are labelled as A1.1, A1.2 and A1.3. Machines are
 391 grouped into workcentres, where a machine can belong to
 392 only one workcentre. Each workcentre can process a number
 393 of operations, where an operation can also belong to only
 394 one workcentre. Thus the machines in a workcentre can be
 395 considered as a group of parallel machines that process the
 396 same operations. PEGS uses search heuristics to find a solu-
 397 tion. When presented with a scheduling task a number of
 398 dispatch heuristics are selected depending on the objective
 399 type and features of the problem. Each is then run and the
 400 best ordering retained. A search strategy is then used to refine
 401 the schedule and can be one of tabu search, simulated anneal-
 402 ing or beam search. The system can be used to schedule for
 403 single machines, parallel machines, job shops or flow shops.

404 For flow shop and job shop problems, the Shifting Bot-
 405 tleneck algorithm is used to generate a solution in the man-

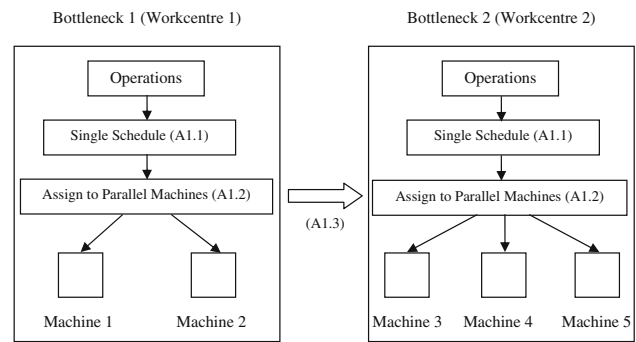


Fig. 1 Basic architecture used in PEGS. Each workcentre can be a bot-
 tleneck and each bottleneck is balanced in turn. Knowing the operations
 to be performed on each bottleneck, we first generate a schedule as if
 there were only a single machine in the workcentre. The operations are
 then assigned to the parallel machines in this order. The ordering on
 one bottleneck may influence the ready times on another

ner described in Section “The shifting bottleneck algorithm”.
 (A1.3 in Fig. 1). The solution at each bottleneck is obtained
 from a slightly modified version of the scheme suggested in
 Morton and Pentico (1993). A schedule is firstly generated for
 all operations on the bottleneck as if it was a single machine
 (A1.1 in Fig. 1). When calculating completion times (used to
 calculate the objective) for this step we then take into account
 the number of parallel machines in the workcentre. The opera-
 tions are assigned to each parallel machine in sequence to
 give a very general idea of possible completion times. This
 is not the final assignment and does not consider different
 machine speeds, but gives improved completion times for the
 single schedule ordering. For example, if the first two opera-
 tions in the single machine schedule are assigned to different
 machines, they may be given the same completion times. The
 completion times if just considering one machine would of
 course be different as one would be scheduled after the other.
 These estimated completion times are then used to calculate
 the objective for the single machine ordering and the best
 ordering retained. We expect this technique to be particu-
 larly effective when measuring the earliness/tardiness objec-
 tive (operations should be neither too early nor too late). The
 operations are then actually assigned to the parallel machines
 in the order of the single machine schedule, in the most eco-
 nomic manner (A1.2 in Fig. 1). We have two algorithms to do
 this. The first simply assigns the operation to the machine that
 can process it first. The second algorithm tries to place simi-
 lar operations together on individual machines. This second
 algorithm is good for minimising waste if environmental fac-
 tors are considered. This architecture is clearly centralised.
 A single algorithm considers all machines in a workcentre
 together. The bottlenecks must also all be processed to-
 gether. This leads to more complex algorithms to process the
 information, but the information is all present in one place
 and there is little need for communication between different

441 parts of the system. In the distributed system described in the
 442 next section there is substantial need for communication between
 443 the agents. So while the distributed solution provides
 444 simpler individual problems, there is increased complexity
 445 through the communications.

446 Distributed architecture

447 In PEGSAgent there are agents to represent machines and
 448 jobs. A machine agent represents a single machine. It is responsible
 449 for finding the best schedule for that machine. There is also a machine mediator agent that controls some global
 450 operations required on all machines. The machine mediator
 451 will create the machine agents and also hold global machine
 452 information, such as which machine processes which operations.
 453 A job agent is responsible for finding the best schedule
 454 for the operations in its job. There is also a job mediator agent
 455 that controls global operations required on all job agents.
 456 The job mediator creates the job agents and also determines
 457 which job agent will try to schedule the next operation. The
 458 actual scheduling process is conducted between the machine
 459 and job agents. The negotiation protocol used here is the
 460 Contract Net protocol (FIPA 2002). Figure 2 shows the main
 461 architecture used.

462 There is one main process which is used to generate a
 463 schedule and there are then two variations on this. In both
 464 variations, the job mediator generates and initialises the job
 465 agents and the machine mediator generates and initialises
 466 the machine agents. In the first step of the process to generate
 467 a new schedule, the job mediator determines the order
 468 in which the operations should be scheduled. It does this by
 469 generating an ordering for each workcentre using one of the
 470 search heuristics for the single machine phase of the Shifting
 471 Bottleneck algorithm described above (A2.1 in Fig. 2).
 472 The operation placed first in this ordering is then given an
 473 *order value* of 1 and so on. These order values are sent to
 474 each job agent for each operation (A2.2 in Fig. 2). The job
 475 mediator then asks each job agent in turn to return the order
 476 value for the next operation that it needs to schedule. The
 477 operation with the lowest order value is given permission to
 478

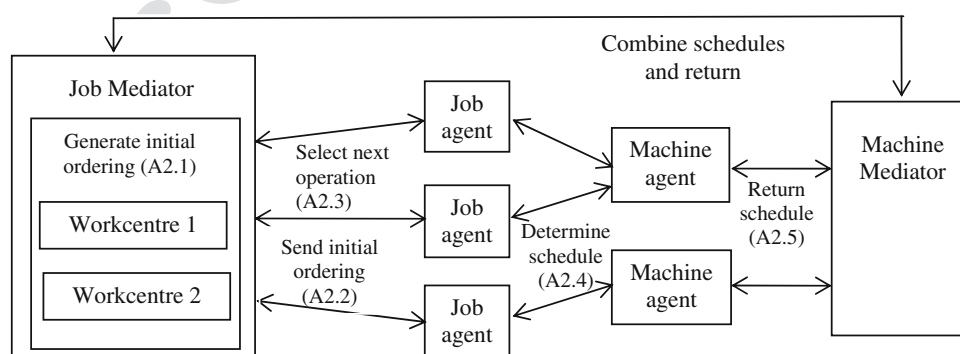
479 be scheduled next (A2.3 in Fig. 2). Note that, within an individual
 480 job, the operations are required to be processed in a certain
 481 sequence to produce that product, and this cannot be over-riden
 482 by preferences due to order values.

483 When a job agent is given permission to schedule its next
 484 operation, it retrieves the addresses of the machines that can
 485 process it and asks each in turn for a schedule time and evaluation.
 486 This negotiation is carried out using the Contract Net protocol.
 487 In this protocol, a job agent will ask the machine agents for times
 488 at which they can schedule its operation. When the machine agents
 489 reply, the job agent evaluates all of the replies and chooses the best
 490 one. It accepts the best proposal and rejects the rest. The accepted
 491 machine agent is then asked to actually schedule the operation at the
 492 time that it specified (A2.4 in Fig. 2). The machine agents determine
 493 the best time that they can schedule the operation taking account
 494 of their existing schedules. A number of factors are used to evaluate
 495 a time slot. These include the actual time and date, the evaluation
 496 of the objective for the machine if that slot is selected and also
 497 some budgetary factors are considered. Budgets are only considered
 498 if time and objective evaluations do not indicate a winner. We
 499 intend to look further at the budget and bidding processes at a later
 500 stage.

501 In this way, all of the operations are eventually assigned to
 502 a machine. When all operations have been assigned, the job
 503 mediator asks the machine mediator to combine the partial
 504 schedules from each machine agent and return this as the final
 505 schedule (A2.5 in Fig. 2). So a search heuristic is used to generate
 506 the initial ordering, to determine the order in which the operations
 507 are allowed to be scheduled. When a machine is then asked to
 508 schedule an operation it uses a local sort to determine the best
 509 position. It tries out each possible slot from the earliest legal
 510 date to the end of its schedule. It places the new operation in
 511 each slot and re-evaluates its objective. The slot that produces
 512 the best objective is returned as the proposal from that machine.
 513

514 The sorting process is part of A2.4 in Fig. 2. One interesting
 515 feature to notice about this sorting process is that it is constructive.
 516 Beginning from no operations on a machine, the count is incremented
 517 one at a time as the schedule is created. If, eventually, there are
 518 five operations on a machine,
 519

Fig. 2 Diagram illustrating the agent interactions to generate a schedule



520 the number of sort iterations required may be something like
 521 $1+2+3+4+5$ for the different scheduling requests on the
 522 machine. This is a lot less than using a search strategy which
 523 would have to deal with the whole schedule during each itera-
 524 tion and for a possibly large number of iterations. The Shif-
 525 ting Bottleneck approach uses the search strategies and is an
 526 iterative process, so searches are performed several times.
 527 The agent-based approach is much quicker as there is only
 528 one search process at the start. This will be shown to dra-
 529 matically reduce search times for a job shop environment.
 530 The advantage is not so good for other environments such as
 531 a flow shop. In this case the centralised approach performs
 532 only one search for each bottleneck and so the agent-based
 533 approach performs an extra sort on the machines in addition
 534 to this. However, for a generic system like PEGSAgent, since
 535 scheduling job shops takes a lot longer than scheduling flow
 536 shops, the advantage for job shops would out-weigh the time
 537 lost on flow shop problems.

538 Having described the basic scheduling process, we now
 539 examine the two variations mentioned above. When a new
 540 operation is inserted into a slot in an existing schedule, it
 541 may change the times of operations that have already been
 542 scheduled. Two approaches have been tried to cope with
 543 this. The first approach is to remove all operations whose
 544 times are affected and then try to re-schedule them again on
 545 some machine. This is similar to the idea of [Boccalatte et al.](#)
 546 (2004), who give the operation to be re-scheduled a favour-
 547 able order value to ensure it is re-scheduled relatively soon
 548 after being moved. However, we found some problems with
 549 this approach. There was a tendency for the scheduling pro-
 550 cess to cycle, when an operation would be inserted early in an
 551 existing schedule. There would then be a ‘knock-on’ effect to
 552 move later operations, which would be re-scheduled on some
 553 other (or the same) machine. This might then move other
 554 operations which follow the new position, which would be
 555 re-scheduled on some other (or the same) machine, etc. This
 556 would particularly be the case if the operations being sched-
 557 uled were very similar to each other. To prevent this cycling
 558 a maximum iteration count was enforced. If any operations
 559 were re-scheduled a maximum count number of times, they
 560 would then be added in a place that did not affect any existing
 561 schedule. However, this modification resulted in operations
 562 being added at the end of the existing schedule. The test sec-
 563 tion will show that while some reasonable schedules were
 564 obtained, another approach proved slightly better.

565 In a second approach, when an operation was inserted at
 566 some intermediate position in a machine schedule, the times
 567 of the operations that came after it on that machine were
 568 pushed forwards to accommodate the new operation. The
 569 times of any dependent operations (due to product sequence
 570 requirements) on different machines were also pushed for-
 571 wards. However, in the case of workcentres with parallel
 572 machines, any of the affected operations were also permitted

573 to be re-scheduled on a similar machine so long as it did not
 574 affect the existing schedule on that machine. If an operation
 575 that was pushed forward could be moved to a more favour-
 576 able position on a different machine without affecting its
 577 existing schedule, then this would be allowed.

578 Comparison with other systems

579 The original aims for developing this system included pro-
 580 vision to account for environmental factors in the schedu-
 581 ling process. This included optimising with regard to waste
 582 and energy, as well as cost. Another aim was to produce a
 583 generic system which would be adaptable to a wide range
 584 of scheduling tasks. The main manufacturing base in Nor-
 585 thern Ireland is SMEs and so a flexible system that could be
 586 used in different scenarios, but would not necessarily have
 587 to process very large schedules, was the target application.
 588 For these reasons, search heuristics were considered accep-
 589 table. However, after looking at other systems and through
 590 practical experience with manufacturer’s and their particu-
 591 lar requirements, many other useful features were added to
 592 the system. We also reviewed a range of currently available
 593 commercial and academic programs. In comparison to the
 594 commercial systems in common use at local companies, our
 595 system appears to have several novel features. The constraint
 596 options in PEGS are similar to those in many systems, but
 597 whereas it is common to use dispatch heuristics for the whole
 598 scheduling process, we prefer to use search heuristics for
 599 the main process. We have also now implemented the agent-
 600 based version. The inclusion of environmental and economic
 601 features is also new. We found other systems that offer the
 602 overlap or ‘accumulation’ processing options, but none seem-
 603 ed to provide our ‘weak’ beside constraint. In summary,
 604 while we found many of the features of PEGS in other sys-
 605 tems, we did not find any other system that offered all of the
 606 features that we have included.

607 Having a typical modern graphics-based user interface,
 608 we imagine that our system should be relatively easy to use,
 609 although help will be required to use the various additional
 610 features that are available. This comes in the form of a user
 611 manual and online help. The most significant task is in setting
 612 up the initial environment. For this a user needs to specify
 613 their shop floor layout and the operations that each machine
 614 can process. Thus, details of each machine must be entered
 615 and then the types, costs and times for processing each opera-
 616 tion in each workcentre needs to be specified. Product details
 617 can then be entered as a sequence of operations that can be
 618 constrained in any allowed way, including the overlap of the
 619 processing of individual operations. Processing details are in
 620 time units to process a single item. The product details then
 621 specify the number of items per operation. Once the initial
 622 details are entered however, they can be saved to an XML

623 file and re-loaded each time the system is used. If they are
 624 relatively permanent then this process only needs to be done
 625 once. The system also tries to be helpful, by providing all
 626 stored information in the form of combo-box options when
 627 required, and even indicating the order in which to enter infor-
 628 mation by only enabling the options that are legal for the next
 629 stage. To make daily use of the system, the user then only
 630 needs to enter the details of the new jobs to schedule. It is also
 631 possible to save schedules and re-load them at the next sched-
 632 uling stage. Old schedules can be updated and re-scheduled
 633 with new jobs, where completed jobs will be removed and the
 634 new jobs integrated. This allows for some level of continuous
 635 scheduling, even though the system is not a dynamic online
 636 one. We provide an interactive Gantt chart, giving a clear
 637 schedule layout and allowing for interactive re-scheduling.

638 Testing the two approaches

639 In this section we describe some tests performed to illustrate
 640 the advantages of the two different agent approaches. The
 641 tests considered both solution quality and execution times.

642 Benchmark datasets

643 The first set of tests compares the quality of the two agent-
 644 based approaches and the conventional program using
 645 well-known benchmark datasets. The values given for the
 646 ‘Optimal objective’ in Table 1 are the best published results
 647 which have been achieved to date. Our generic system does
 648 not produce such high quality schedules but it has not been
 649 ‘tuned’ to any particular problem type or dataset. As a conse-
 650 quence, the individual evaluations from PEGS are not so
 651 interesting, but the results demonstrate that PEGS works well
 652 for a range of different problems. Table 1 lists some datasets
 653 which have been used to test the scheduling quality and the
 654 best objective values from PEGS averaged over a small num-
 655 ber of runs.

656 Generally, the objective values obtained from PEGS were
 657 not as good as the best published values, though there were
 658 three cases in the Purdue data where the PEGS objective
 659 was better. The Flexible Manufacturing System example is
 660 also interesting. This system allows any of the machines to
 661 process any of the operations but not all machines process
 662 all operations. This was implemented in PEGS as a Parallel
 663 Machine configuration (single group of parallel machines)
 664 where not all machines processed all operations. On aver-
 665 age, the PEGS Shifting Bottleneck algorithm performed
 666 just slightly better than PEGSAgent2, while PEGSAgent1
 667 performed worst. This suggests that the second agent-based
 668 approach produces good quality solutions compared to our
 669 implementation of the centralised approach. All schedules
 670 were solved in relatively short amounts of time (just a few

seconds), so execution time was not a problem. These results
 show that while PEGS and PEGSAgent may not produce
 optimal solutions, they will tend to produce good solutions
 in most cases.

Random datasets

The three approaches were also tested on randomly gener-
 ated datasets for flow shop and job shop configurations.
 The objective measured was weighted makespan (because
 a search strategy is used for this objective). In all cases the
 search strategy used was tabu search and each measurement
 was averaged over three test runs.

Flow shop tests

This set of tests was for three different flow shop configura-
 tions. The objective evaluation and the execution times are
 given in Table 2 for different factory configurations. Flow
 Shop 1 (FS1) has three workcentres (WC), 20 jobs (J) and 60
 operations (Op). Flow Shop 2 has a five workcentres, 30 jobs
 and 150 operations. Flow Shop 3 has seven workcentres,
 25 jobs and 175 operations. Each workcentre contained a
 number of parallel machines. Flow Shop 1 had 11 machines,
 Flow Shop 2 had 18 machines and Flow Shop 3 also had 18
 machines. Each test run was for 100,000 iterations at each
 search step.

The results show that execution time is not greatly affected
 by the extra sort of the agents. Clearly this is a much quicker
 process than the search process. To extend the analysis to
 reflect more practical situations, some tests were conducted
 with heavily constrained data. This data included setup times,
 waste costs and shift and time constraints. In these cases
 the agent sort took longer, but, for the size of datasets we
 are measuring here, it was still measured in seconds. When
 scaling up to larger datasets, the sort with heavily constrained
 data would require a more significant amount of extra time.

In two of the three tests PEGSAgent2 produced the best
 objectives, while in the other test it was PEGSAgent1. This
 outcome supports a decision to use an agent-based approach.
 It is possible that the PEGSAgent1 is better in the first set
 of tests because there are fewer operations. In this case more
 operations will be ‘properly’ scheduled before the maximum
 iteration count is reached and the remaining are placed at the
 end.

Job shop tests

This set of tests was for three different job shop configura-
 tions. The objective evaluation and execution times are given
 in Table 3 for the different schedule configurations. Job Shop
 1 (JS1) has three workcentres (WC), 20 jobs (J) and 80 ope-
 rations (Op). Job Shop 2 has five workcentres, 30 jobs and

Table 1 List of benchmark datasets used to test the quality of the different approaches

Benchmark dataset ^a	Objective type	Shop type	Optimal objective	PEGS objective	PEGSA1 objective ^b	PEGSA2 objective ^b
abz5	Makespan	Job shop	1234	1296	1352	1307
abz6	Makespan	Job shop	943	1018	981	984
abz7	Makespan	Job shop	655	772	809	774
la19	Makespan	Job shop	842	998	951	951
la20	Makespan	Job shop	902	964	999	975
flcmax_20_15_3	Makespan	Flow shop	4437	4393	4713	4486
flcmax_20_15_4	Makespan	Flow shop	3779	3865	4095	4056
flcmax_20_15_6	Makespan	Flow shop	4144	4128	4227	4163
fl_20_15_1_1_2	Lateness	Flow shop	2833	3025	3033	3033
fl_20_15_1_1_3	Lateness	Flow shop	2322	2608	2789	2489
fl_20_15_2_1_5	Lateness	Flow shop	3651	3692	3728	3633
fl_20_15_2_1_6	Lateness	Flow shop	3360	3507	3516	3419
Day1	Makespan	Flexible flow shop	760	791	826	831
Day2	Makespan	Flexible flow shop	770	826	837	842
Day3	Makespan	Flexible flow shop	770	827	818	833
Day4	Makespan	Flexible flow shop	785	820	857	827
Day5	Makespan	Flexible flow shop	961	986	1031	1031
Day6	Makespan	Flexible flow shop	667	701	706	706
Dataset1	Makespan	Flexible manuf.	420	391	411	441

The optimal objectives and the objective values we found by each approach are given

^a abz is Adams et al. (1988), la is Lawrence (1984), flcmax are the makespan datasets from Purdue (in Dimirkol et al. 1998), fl are the lateness datasets from Purdue (in Dimirkol et al. 1998), Day is Wittrock (1988) and Dataset1 is Kumar et al. (2003)

^b PEGSA1 and PEGSA2 refer to the PEGSAgent program operating with the first and second variations described in the text

Table 2 Comparison of objective values and execution times (s) from PEGS variants (100,000 iterations on each search and varying factory configurations)

Dataset		Program version					
		PEGS		PEGSA1		PEGSA2	
		Objective	Time	Objective	Time	Objective	Time
FS1	WC: 3 J: 20 Op: 60	16,124	11	15,987	11	16,115	12
FS2	WC: 5 J: 30 Op: 150	63,109	25	66,366	25	58,938	25
FS3	WC: 7 J: 25 Op: 175	59,121	31	58,728	30	55,100	32

FS is flow shop, WC is number of workcentres, J is number of jobs and Op is number of operations

150 operations. Job Shop 3 has seven workcentres, 25 jobs and 125 operations. Each workcentre consisted of a number of parallel machines. For Job Shop 1 there was a total of 11 machines, for Job Shop 2 a total of 15 machines and for Job Shop 3 a total of 18 machines. Each test run was for 100,000 iterations for each search step.

These results show a clear superiority of PEGSAgent1 and 2 over the centralised approach in PEGS. The agent-based approaches produced better objectives, with the second version being better in all three tests. Considering the execution times, the agent-based approaches are 6–15 times faster than the centralised approach with the greatest advantage associa-

ted with the larger problems. These tests also show that for the centralised system (PEGS) the number of workcentres is a more important influence on execution time than the number of operations. The third test had fewer operations than the second but more workcentres. Each workcentre requires its own search and, coupled with balancing of more bottlenecks, the total number of searches is greater. As the agent-based approach only performs one search at the start there are no problems with extra iterations and so it can produce schedules for JS2 and JS3 in much the same time.

From the flow shop and job shop results, it would appear that the second agent-based approach, PEGSAgent2, is the

Table 3 Comparison of objective values and execution times (s) from PEGS variants (100,000 iterations on each search and varying factory configurations)

Dataset	Program version	Program version					
		PEGS		PEGSA1		PEGSA2	
		Objective	Time	Objective	Time	Objective	Time
JS1	WC: 3 J: 20 Op: 80	27,917	89	24,053	15	23,373	15
JS2	WC: 5 J: 30 Op: 150	131,710	266	124,658	27	108,075	27
JS3	WC: 7 J: 25 Op: 125	78,802	404	59,636	26	57,788	26

JS is job shop, WC is number of workcentres, J is number of jobs and Op is number of operations

742 most consistent in terms of quality and execution speed and
743 would therefore be the preferred option.

744 Conclusions

745 PEGS is a generic production scheduling system. The initial
746 implementation used a centralised solution based on search
747 strategies and the Shifting Bottleneck algorithm, and has pro-
748 ved to reliably provide good schedules for a wide range of
749 flow shop or job shop problems. However, this technique is
750 necessarily slow. One possible alternative is an agent-based
751 approach and we have suggested a basic framework for using
752 the agents. This includes an initial search and then a much
753 shorter sort on the agents. This method is a similar idea to
754 Bocalatte et al. (2004) but there are several differences. We
755 use a different method for calculating the initial order. They
756 use the job slack time to determine the ideal job start time and
757 also use a probability function to determine if the job agent
758 then issues a call for proposals in the Contract Net protocol
759 to initiate a schedule. The machine agents then order the job
760 proposals based on the bid values. They also re-schedule jobs
761 in a different way, by assigning a higher priority to the jobs
762 being re-scheduled and then re-calculating their bid values.
763 The Contract Net protocol seems to cover their whole sched-
764 uling process. Their system is for just-in-time manufactur-
765 ing where jobs arrive dynamically and are scheduled as they
766 arrive. Our system is currently more suited to a situation
767 where there are a number of jobs that need to be scheduled
768 and they are all scheduled at one time, say at the start of a
769 week.

770 We have suggested two variations on using the agent-
771 based approach. These both treat the agents as individual
772 entities with no communication between them to try to obtain
773 a better global schedule. The machine agents try to minimise

774 the schedule for their machine only and do not consider the
775 schedule on other machines. This could reasonably be expect-
776 ed to produce good results, for if each machine agent tries
777 to minimise its schedule this will mean the global objective
778 will also be minimised. Shen (2002) writes that there are also
779 some agent systems where the agents communicate with each
780 other in an attempt to minimise some global objective. We
781 have also considered this approach and are testing a third
782 variation that takes this into account. In the third variation,
783 when a schedule is calculated for one machine, the schedules
784 on all machines are updated. All machines then calculate their
785 objectives and these are returned as well as the local machine
786 objective. It is then possible to consider the objectives of all
787 machines. If the worst of these is better than the current best
788 (in terms of its impact on the overall objective), then even if
789 the local objective is worse, this schedule may be preferred.

790 The test results show that agent methods, compared to
791 our centralised system, can produce schedules that are only
792 slightly worse on benchmark datasets and actually better on
793 our own random datasets. The agents can also save a large
794 amount of processing time, in some cases by a factor of 10
795 or more for job shops. This would mean that the agent-based
796 system would be able to handle larger numbers of jobs. It
797 seems that agents may not be able to produce optimal solu-
798 tions but can produce good solutions, though Vancza and
799 Markus (2000) show that near optimal solutions may be
800 achievable in some cases, and we also found this. The lack of
801 information that each agent possesses may make it difficult
802 to produce optimal solutions.

803 We would suggest that in a generic or commercial sys-
804 tem of this type, an agent-based approach would be a good
805 option. This is because these types of systems may be more
806 interested in providing a range of features than in producing
807 optimal solutions. If optimality is not the over-riding issue,
808 the flexibility and speed of the agent-based approach may
809 be preferred for today's dynamic scheduling environment.

810 A demo version of the program is available for downloading
811 from our Environmental Modelling Group website (Stewart
812 2006). This includes PEGS and PEGSagent2. An additional
813 distributed program will allow operation of the distributed
814 PEGS version.

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